

When we did our analytic analysis of the constraint conditions between the accelerations of objects 1 and 2, we came up with the condition that a_1 was equal to minus 2 a_2 .

Now let's do something which we call a virtual displacement argument.

Suppose that b and 2 move down a certain amount.

Let's imagine-- and I'm going to draw in a different color, too-- so we have object 2, and pulley 2 has moved down.

Now, this object has displaced by distance Δy_2 , which is also equal to Δy_b because they're connected.

Now, what happens when the system does that, is our rope has to extend downwards around this pulley and come back up.

And that means that the rope that object 1 has been foreshortened by not just Δy_2 , but on both sides, Δy_2 and Δy_2 , object 1 has displaced up by that amount.

So we'll just make this so we can draw it in a reasonable way.

So what we see here is that Δy_1 is equal to-- now notice, if 2 goes down, by Δy_2 , then Δy_1 -- which is this whole distance-- is a negative quantity.

And it's going upwards.

And so we see that that's minus 2 Δy_2 .

And if we took two derivatives-- or displacement and then look at the change in displacement-- we would see that this implies that the acceleration of 1 is minus 2 a_2 .

But let's come back to our two conditions for length and see the same thing here.

Because Δl_2 is 0, this tells us that Δy_2 is equal to Δy_d .

So we'll write minus equals 0.

And that was our condition that the block and 2 were moving together.

And up here, we see that, because Δl_1 is also 0, this implies-- and now I'll make that substitution that Δy_b is equal to Δy_2 -- that 2 Δy_2 here and here plus Δy_1 has to be 0 coming from that piece.

And so we see that Δy_1 is minus 2 Δy_2 .

Which is what our virtual displacement argument showed us.

And again, if you take two derivatives here, we have that recall that, in the simplest way, that the velocity is dy/dt .

And the acceleration, a_1 , is d^2y/dt^2 .

Then, this same proportionality is maintained under the two derivatives.

And that's another way of thinking about how to get the relationship between the accelerations.

But you have to be extremely careful about that sign because this 2 goes in the positive direction, 1 will go in the negative direction.