

LIST COMPREHENSION, FUNCTIONS AS OBJECTS, TESTING, DEBUGGING

(download slides and .py files to follow along)

6.100L Lecture 12

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LIST COMPREHENSIONS

LIST COMPREHENSIONS

- Applying a **function to every element of a sequence**, then creating a new list with these values is a common concept

- Example: *New list*

```
def f(L):  
    Lnew = []  
    for e in L:  
        Lnew.append(e**2)  
    return Lnew
```

Function to apply

- Python provides a concise one-liner way to do this, called a **list comprehension**
 - Creates a new list
 - Applies a function to every element of another iterable
 - Optional, only apply to elements that satisfy a test

```
[expression for elem in iterable if test]
```

LIST COMPREHENSIONS

- Create a **new** list, by applying a function to every element of another iterable that satisfies a test

```
def f(L):  
    Lnew = []  
    for e in L:  
        Lnew.append(e**2)  
    return Lnew
```

New list

Look at every element

Function to apply

New list

```
Lnew = [e**2 for e in L]
```

LIST COMPREHENSIONS

- Create a **new** list, by applying a function to every element of another iterable that satisfies a test

```
def f(L):  
    Lnew = []  
    for e in L:  
        Lnew.append(e**2)  
    return Lnew
```

```
def f(L):  
    Lnew = []  
    for e in L:  
        if e%2==0:  
            Lnew.append(e**2)  
    return Lnew
```

New list

*Function to apply
only if test is true*

```
Lnew = [e**2 for e in L]
```

LIST COMPREHENSIONS

- Create a **new** list, by applying a function to every element of another iterable that satisfies a test

```
def f(L):  
    Lnew = []  
    for e in L:  
        Lnew.append(e**2)  
    return Lnew
```

```
def f(L):  
    Lnew = []  
    for e in L:  
        if e%2==0:  
            Lnew.append(e**2)  
    return Lnew
```

```
Lnew = [e**2 for e in L]
```

New list

```
Lnew = [e**2 for e in L if e%2==0]
```



LIST COMPREHENSIONS

- Create a **new** list, by applying a function to every element of another iterable that satisfies a test

```
def f(L):  
    Lnew = []  
    for e in L:  
        Lnew.append(e**2)  
    return Lnew
```

```
def f(L):  
    Lnew = []  
    for e in L:  
        if e%2==0:  
            Lnew.append(e**2)  
    return Lnew
```

Loop over elements

```
Lnew = [e**2 for e in L]
```

```
Lnew = [e**2 for e in L if e%2==0]
```

LIST COMPREHENSIONS

- Create a **new** list, by applying a function to every element of another iterable that satisfies a test

```
def f(L):  
    Lnew = []  
    for e in L:  
        Lnew.append(e**2)  
    return Lnew
```

```
def f(L):  
    Lnew = []  
    for e in L:  
        if e%2==0:  
            Lnew.append(e**2)  
    return Lnew
```

*Function to apply
only if test is true*

```
Lnew = [e**2 for e in L]
```

```
Lnew = [e**2 for e in L if e%2==0]
```

LIST COMPREHENSIONS

`[expression for elem in iterable if test]`

- This is equivalent to invoking this function (where expression is a function that computes that expression)

```
def f(expr, old_list, test = lambda x: True):  
    new_list = []  
    for e in old_list:  
        if test(e):  
            new_list.append(expr(e))  
    return new_list
```

`[e**2 for e in range(6)]` → `[0, 1, 4, 9, 16, 25]`

`[e**2 for e in range(8) if e%2 == 0]` → `[0, 4, 16, 36]`

`[[e,e**2] for e in range(4) if e%2 != 0]` → `[[1,1], [3,9]]`

YOU TRY IT!

- What is the value returned by this expression?
 - Step1: what are **all values** in the sequence
 - Step2: which **subset of values** does the condition filter out?
 - Step3: **apply the function** to those values

```
[len(x) for x in ['xy', 'abcd', 7, '4.0'] if type(x) == str]
```

FUNCTIONS: DEFAULT PARAMETERS

SQUARE ROOT with BISECTION

```
def bisection_root(x):  
    epsilon = 0.01  
    low = 0  
    high = x  
    guess = (high + low)/2.0  
    while abs(guess**2 - x) >= epsilon:  
        if guess**2 < x:  
            low = guess  
        else:  
            high = guess  
        guess = (high + low)/2.0  
    return guess  
  
print(bisection_root(123))
```

ANOTHER PARAMETER

- Motivation: want a more accurate answer

`def bisection_root(x)` can be improved

- Options?
 - Change epsilon **inside function** (all function calls are affected)
 - Use an epsilon **outside function** (global variables are bad)
 - Add epsilon as **an argument** to the function

epsilon as a PARAMETER

```
def bisection_root(x, epsilon):  
    low = 0  
    high = x  
    guess = (high + low)/2.0  
    while abs(guess**2 - x) >= epsilon:  
        if guess**2 < x:  
            low = guess  
        else:  
            high = guess  
        guess = (high + low)/2.0  
    return guess  
  
print(bisection_root(123, 0.01))
```

KEYWORD PARAMETERS & DEFAULT VALUES

`def` `bisection_root(x, epsilon)` can be improved

- We added `epsilon` as an argument to the function
 - **Most of the time** we want some **standard value**, 0.01
 - **Sometimes**, we may want to use some **other value**
- Use a keyword parameter aka a **default parameter**

Epsilon as a KEYWORD PARAMETER

```
def bisection_root(x, epsilon=0.01):  
    low = 0  
    high = x  
    guess = (high + low)/2.0  
    while abs(guess**2 - x) >= epsilon:  
        if guess**2 < x:  
            low = guess  
        else:  
            high = guess  
        guess = (high + low)/2.0  
    return guess
```

*Default parameter, with
default value of 0.01*

```
print(bisection_root(123))
```

```
print(bisection_root(123, 0.5))
```

*Uses epsilon as 0.01 (the default one in
function def)*

Uses epsilon as 0.5

RULES for KEYWORD PARAMETERS

- In the **function definition**:

- Default parameters must go at the end

- These are **ok for calling a function**:

- `bisection_root_new(123)`
- `bisection_root_new(123, 0.001)`
- `bisection_root_new(123, epsilon=0.001)`
- `bisection_root_new(x=123, epsilon=0.1)`
- `bisection_root_new(epsilon=0.1, x=123)`

- These are **not ok for calling a function**:

- `bisection_root_new(epsilon=0.001, 123) #error`
- `bisection_root_new(0.001, 123) #no error but wrong`

FUNCTIONS RETURNING FUNCTIONS

OBJECTS IN A PROGRAM

```
def is_even(i):  
    return i%2 == 0
```

```
r = 2
```

```
pi = 22/7
```

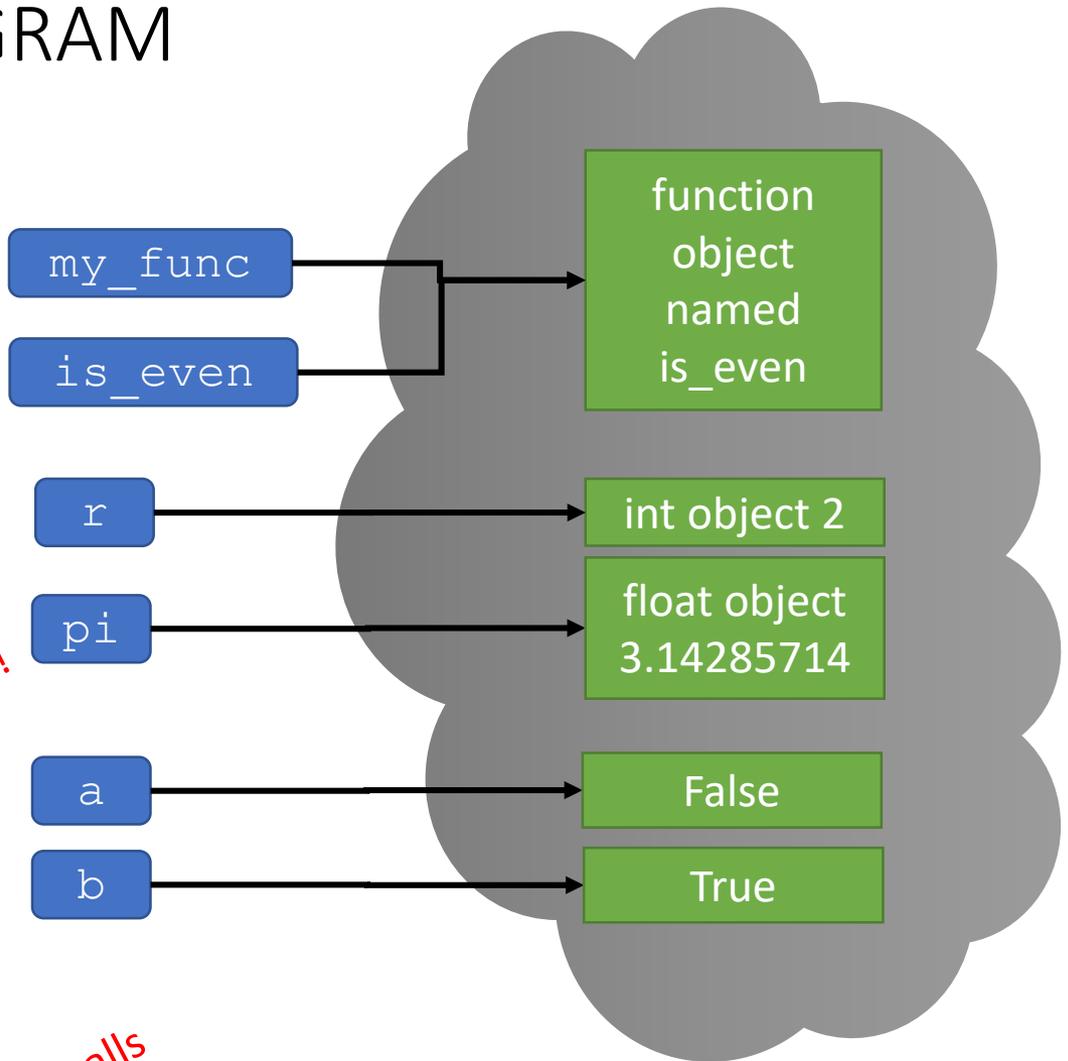
```
my_func = is_even
```

```
a = is_even(3)
```

```
b = my_func(4)
```

**NOT a function
call, just names!**

Function calls



FUNCTIONS CAN RETURN FUNCTIONS

```
def make_prod(a):
```

```
    def g(b):  
        return a*b
```

```
    return g
```

*This is NOT a
function call!*

*This function def is
inside another function.*

```
val = make_prod(2)(3)  
print(val)
```

SAME

```
doubler = make_prod(2)  
val = doubler(3)  
print(val)
```

SCOPE DETAILS FOR WAY 1

```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g  
  
val = make_prod(2)(3)  
print(val)
```

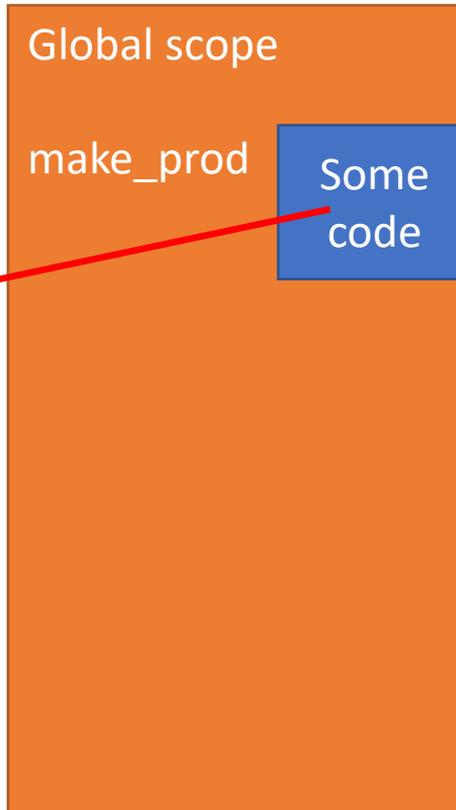
SCOPE DETAILS FOR WAY 1

```
def make_prod(a):
```

```
    def g(b):  
        return a*b  
    return g
```

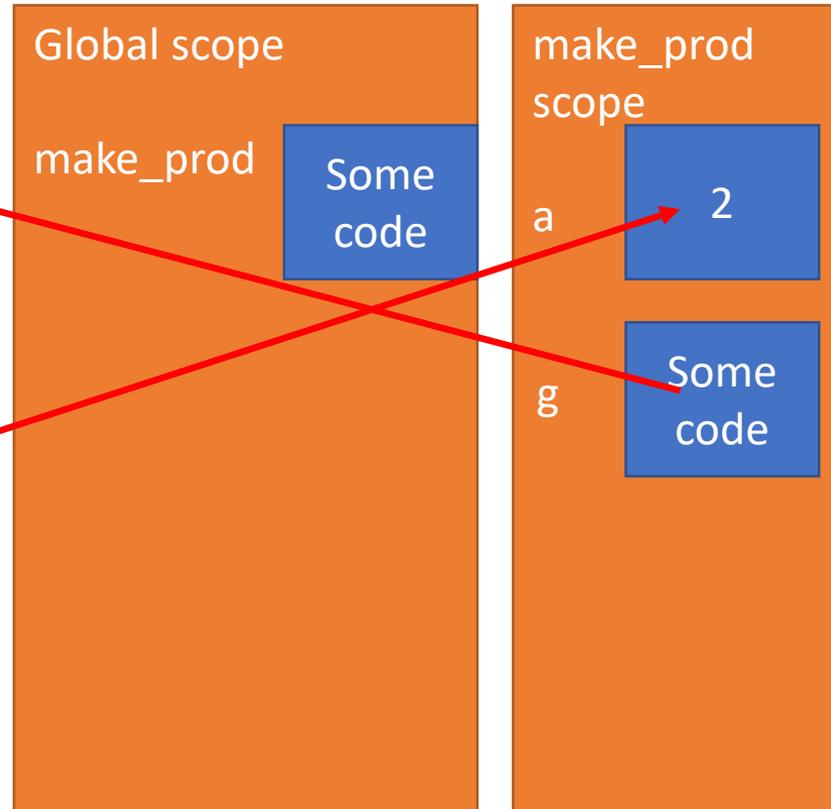
```
val = make_prod(2)(3)
```

```
print(val)
```



SCOPE DETAILS FOR WAY 1

```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g  
  
val = make_prod(2)(3)  
print(val)
```



NOTE: definition of `g` is done within scope of `make_prod`, so binding of `g` is within that frame/scope

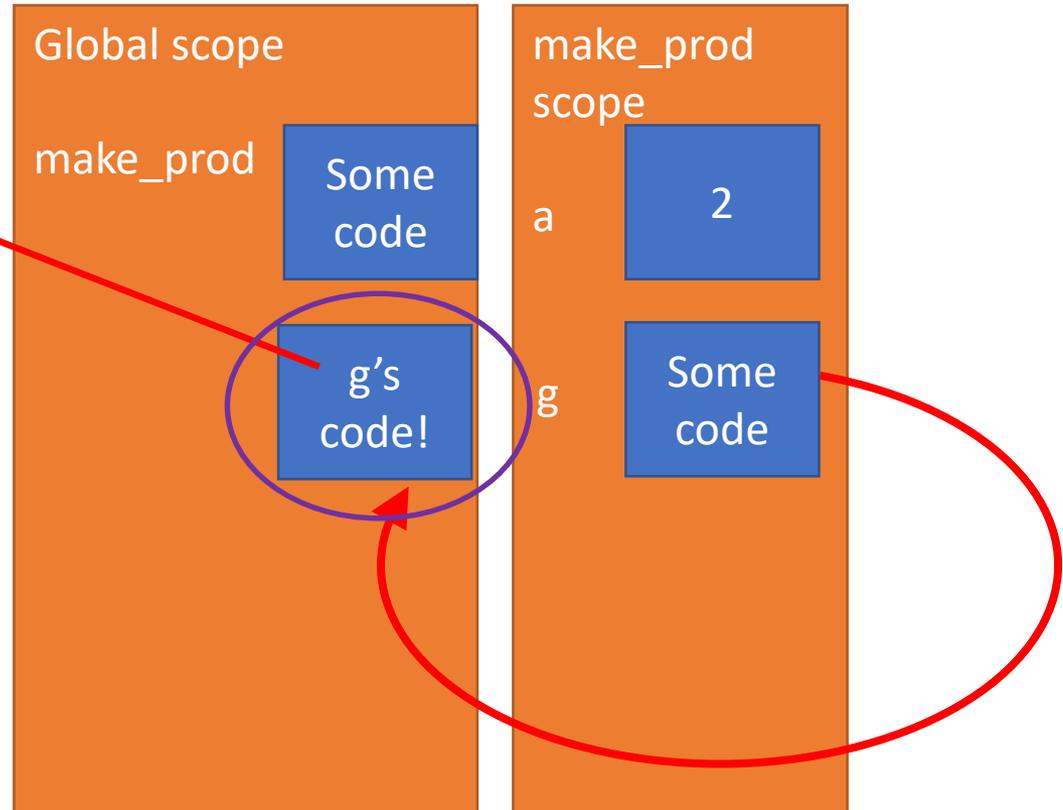
Since `g` is bound in this frame, cannot access it by evaluation in global frame

`g` can only be accessed within call to `make_prod`, and each call will create a new, internal `g`

SCOPE DETAILS FOR WAY 1

```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g  
  
val = make_prod(2) (3)  
print(val)
```

This is g



Evaluating `make_prod(2)` has returned an anonymous procedure

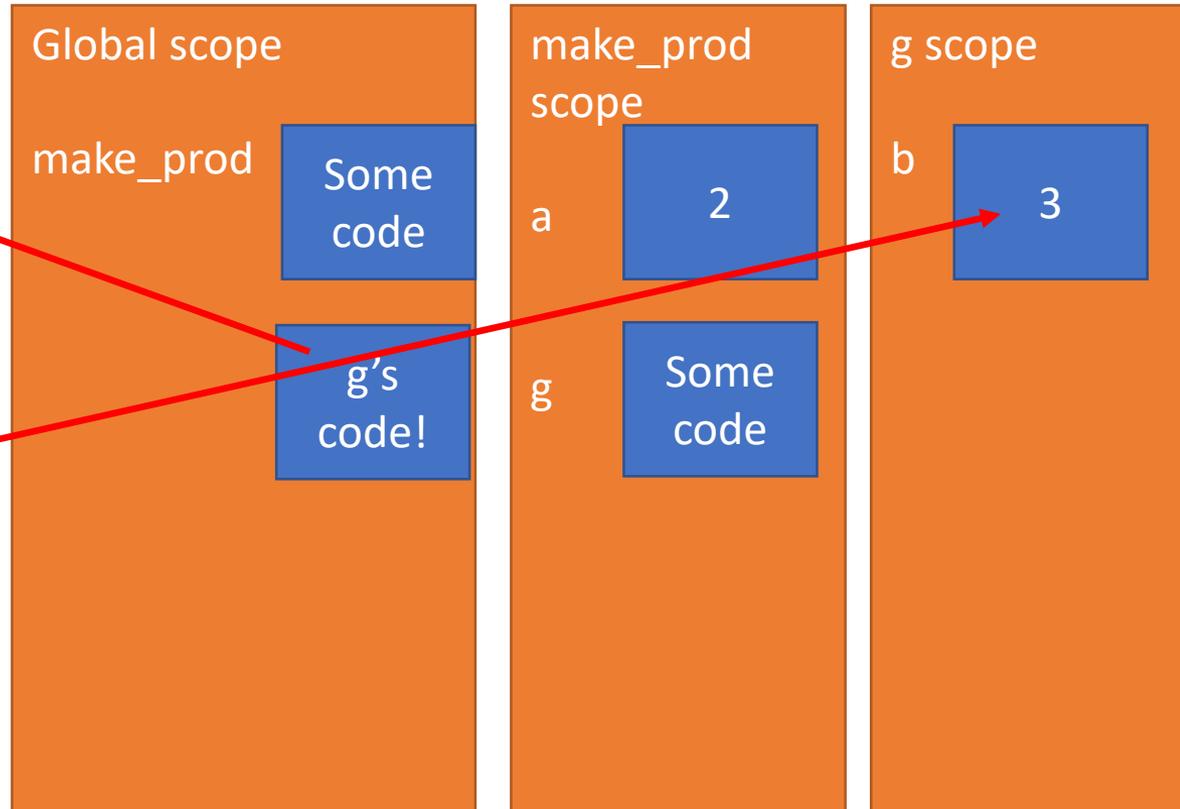
Returns pointer to g code

SCOPE DETAILS FOR WAY 1

```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g
```

```
val = make_prod(2)(3)  
print(val)
```

Call is g(3)

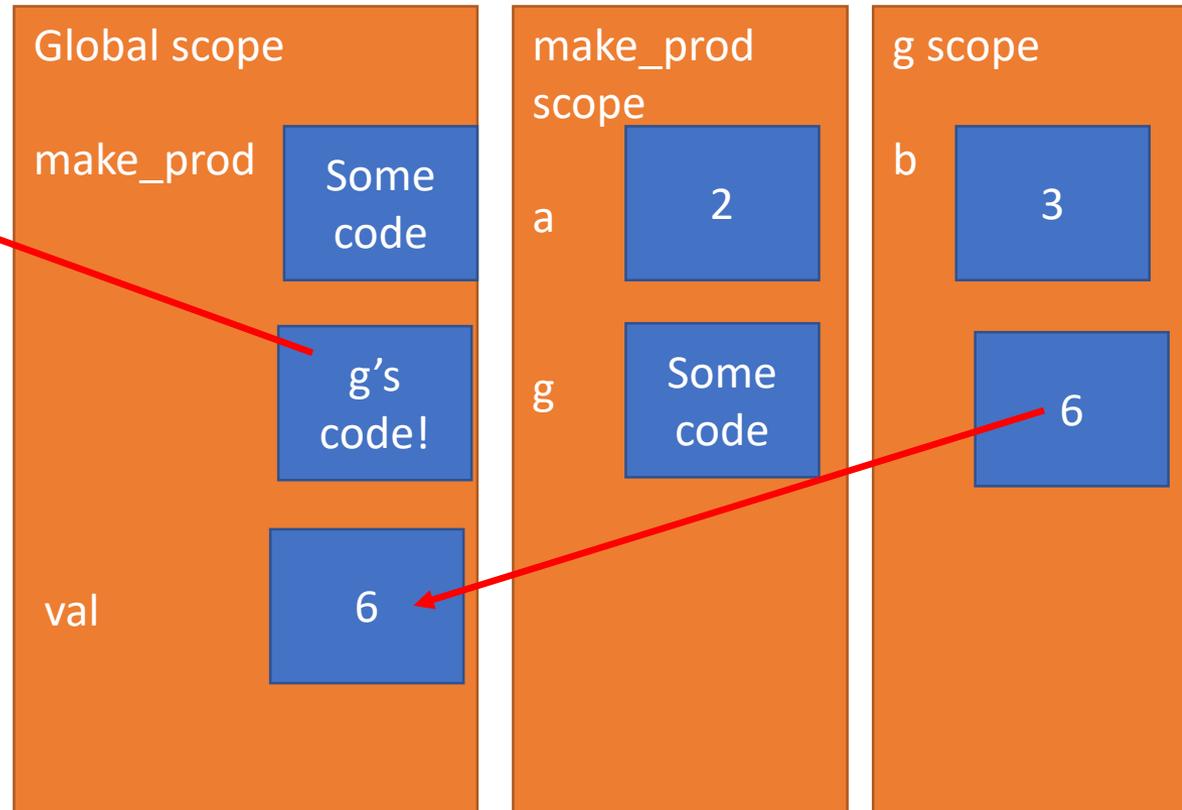


SCOPE DETAILS FOR WAY 1

```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g
```

```
val = make_prod(2)(3)  
print(val)
```

Internal procedure only accessible within scope from parent procedure's call



How does g get value for a?
Interpreter can move up hierarchy of frames to see both b and a values

SCOPE DETAILS FOR WAY 2

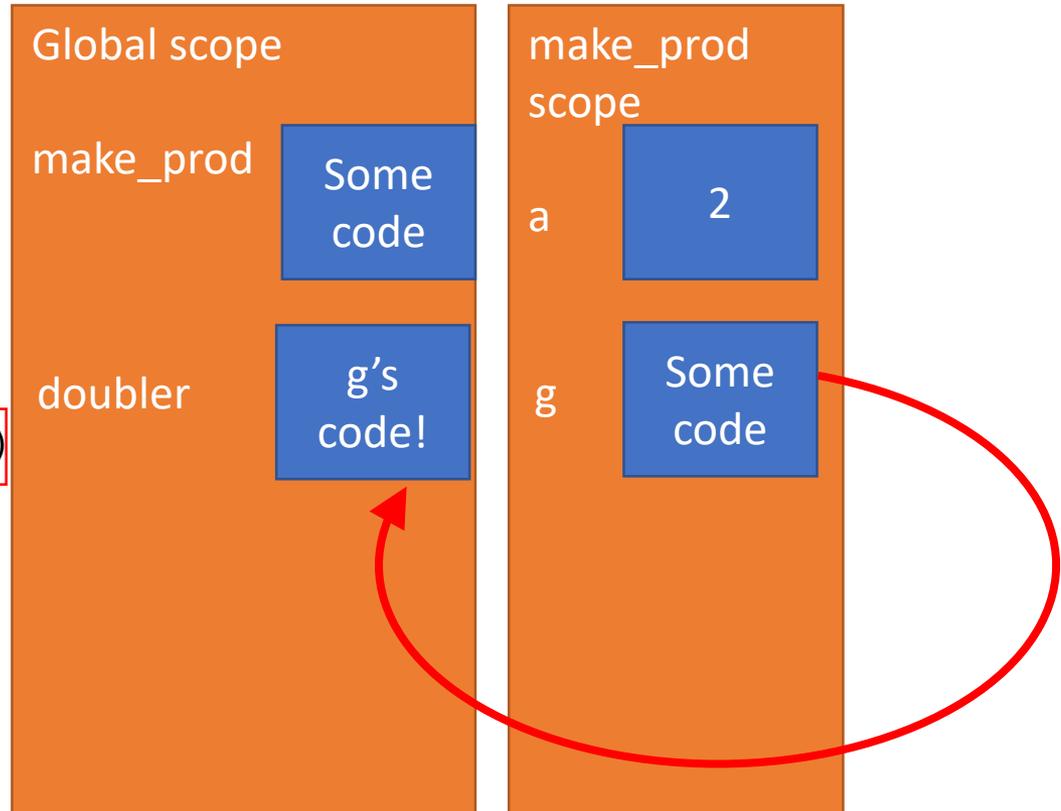
```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g
```

```
doubler = make_prod(2)  
val = doubler(3)  
print(val)
```

SCOPE DETAILS FOR WAY 2

```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g
```

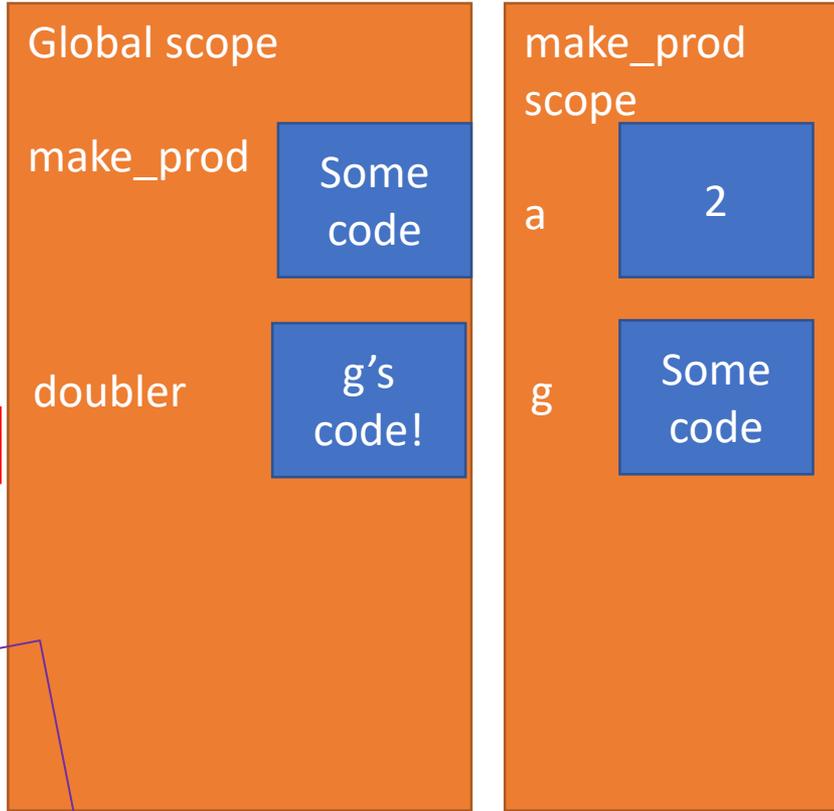
```
doubler = make_prod(2)  
val = doubler(3)  
print(val)
```



SCOPE DETAILS FOR WAY 2

```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g
```

```
doubler = make_prod(2)  
val = doubler(3)  
print(val)
```

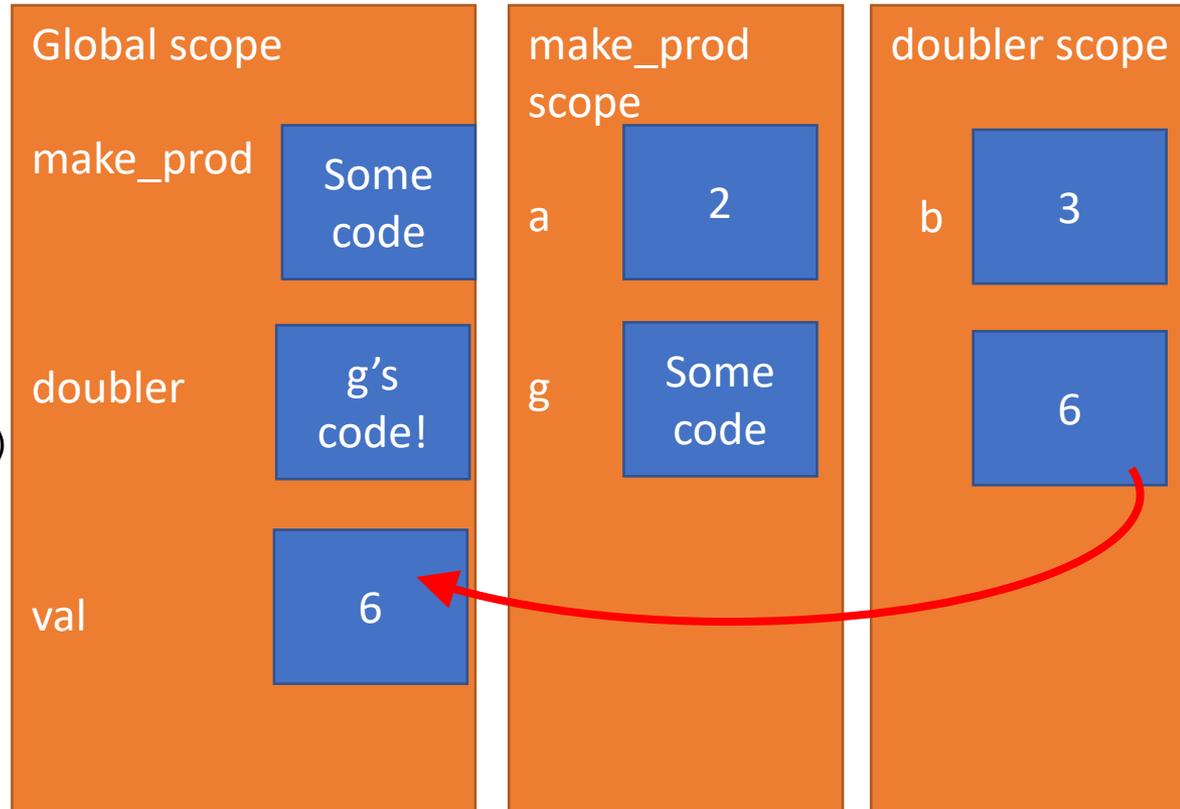


Evaluating `make_prod(2)` has same effect as previous example – `doubler` is a **function object**

SCOPE DETAILS FOR WAY 2

```
def make_prod(a):  
    def g(b):  
        return a*b  
    return g  
  
doubler = make_prod(2)  
val = doubler(3)  
print(val)
```

Now invoking g(3)



Returns value

WHY BOTHER RETURNING FUNCTIONS?

- Code can be **rewritten** without returning function objects
- Good software design
 - Embracing ideas of **decomposition, abstraction**
 - Another **tool** to structure code
- Interrupting execution
 - Example of **control flow**
 - A way to achieve **partial execution** and use result somewhere else before finishing the full evaluation

TESTING and DEBUGGING

DEFENSIVE PROGRAMMING

- Write **specifications** for functions
- **Modularize** programs
- Check **conditions** on inputs/outputs (assertions)

TESTING/VALIDATION

- **Compare** input/output pairs to specification
- “It’s not working!”
- “How can I break my program?”

DEBUGGING

- **Study events** leading up to an error
- “Why is it not working?”
- “How can I fix my program?”

SET YOURSELF UP FOR EASY TESTING AND DEBUGGING

- From the **start**, design code to ease this part
- Break program up into **modules** that can be tested and debugged individually
- **Document constraints** on modules
 - What do you expect the input to be?
 - What do you expect the output to be?
- **Document assumptions** behind code design

WHEN ARE YOU READY TO TEST?

- Ensure **code runs**
 - Remove syntax errors
 - Remove static semantic errors
 - Python interpreter can usually find these for you
- Have a **set of expected results**
 - An input set
 - For each input, the expected output

CLASSES OF TESTS



- **Unit testing**

- Validate each piece of program
- **Testing each function** separately

- **Regression testing**

- Add test for bugs as you find them
- **Catch reintroduced** errors that were previously fixed

- **Integration testing**

- Does **overall program** work?
- Tend to rush to do this

TESTING APPROACHES

- **Intuition** about natural boundaries to the problem

```
def is_bigger(x, y):  
    """ Assumes x and y are ints  
    Returns True if y is less than x, else False """
```

- can you come up with some natural partitions?
- If no natural partitions, might do **random testing**
 - Probability that code is correct increases with more tests
 - Better options below
- **Black box testing**
 - Explore paths through specification
- **Glass box testing**
 - Explore paths through code

BLACK BOX TESTING

```
def sqrt(x, eps):  
    """ Assumes x, eps floats, x >= 0, eps > 0  
    Returns res such that x-eps <= res*res <= x+eps """
```

- Designed **without looking** at the code
- Can be done by someone other than the implementer to avoid some implementer **biases**
- Testing can be **reused** if implementation changes
- **Paths** through specification
 - Build test cases in different natural space partitions
 - Also consider boundary conditions (empty lists, singleton list, large numbers, small numbers)

BLACK BOX TESTING

```
def sqrt(x, eps):  
    """ Assumes x, eps floats, x >= 0, eps > 0  
    Returns res such that x-eps <= res*res <= x+eps """
```

CASE	x	eps
boundary	0	0.0001
perfect square	25	0.0001
less than 1	0.05	0.0001
irrational square root	2	0.0001
extremes	2	1.0/2.0**64.0
extremes	1.0/2.0**64.0	1.0/2.0**64.0
extremes	2.0**64.0	1.0/2.0**64.0
extremes	1.0/2.0**64.0	2.0**64.0
extremes	2.0**64.0	2.0**64.0

GLASS BOX TESTING

- **Use code** directly to guide design of test cases
- Called **path-complete** if every potential path through code is tested at least once
- What are some **drawbacks** of this type of testing?
 - Can go through loops arbitrarily many times
 - Missing paths
- Guidelines
 - Branches
 - For loops
 - While loops

*exercise all parts of a conditional
loop not entered
body of loop executed exactly once
body of loop executed more than once*

*same as for loops, cases
that catch all ways to exit
loop*

GLASS BOX TESTING

```
def abs(x):  
    """ Assumes x is an int  
    Returns x if x>=0 and -x otherwise """  
    if x < -1:  
        return -x  
    else:  
        return x
```

- A path-complete test suite could **miss a bug**
- Path-complete test suite: 2 and -2
- But `abs(-1)` incorrectly returns -1
- Should still test boundary cases

DEBUGGING

- Once you have discovered that your code does not run properly, you want to:
 - Isolate the bug(s)
 - Eradicate the bug(s)
 - Retest until code runs correctly for all cases
 - Steep learning curve
- Goal is to have a bug-free program
- Tools
 - **Built in** to IDLE and Anaconda
 - **Python Tutor**
 - **print** statement
 - Use your brain, be **systematic** in your hunt

ERROR MESSAGES – EASY

- Trying to access beyond the limits of a list

`test = [1, 2, 3] then test[4]` → `IndexError`

- Trying to convert an inappropriate type

`int(test)` → `TypeError`

- Referencing a non-existent variable

`a` → `NameError`

- Mixing data types without appropriate coercion

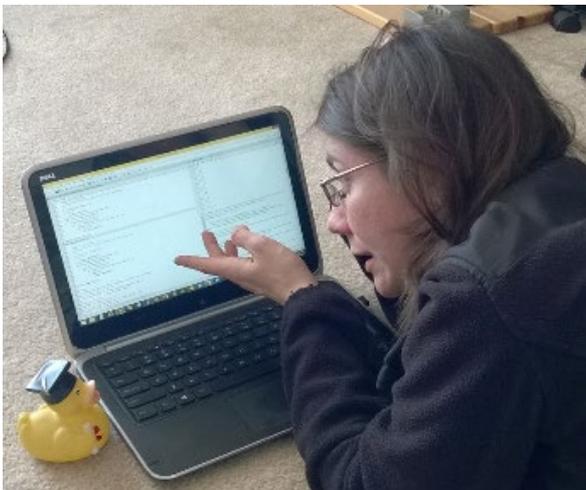
`'3' / 4` → `TypeError`

- Forgetting to close parenthesis, quotation, etc.

`a = len([1, 2, 3]`
`print(a)` → `SyntaxError`

LOGIC ERRORS - HARD

- **think** before writing new code
- **draw** pictures, take a break
- **explain** the code to
 - someone else
 - a rubber ducky



DEBUGGING STEPS

- **Study** program code
 - Don't ask what is wrong
 - Ask how did I get the unexpected result
 - Is it part of a family?
- **Scientific method**
 - Study available data
 - Form hypothesis
 - Repeatable experiments
 - Pick simplest input to test with

PRINT STATEMENTS

- Good way to **test hypothesis**
- When to print
 - Enter function
 - Parameters
 - Function results
- Use **bisection method**
 - Put print halfway in code
 - Decide where bug may be depending on values

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