Work, Heat, and the First Law



If p_{ext} is not constant, then we have to look at infinitesimal changes

surroundings $(\Delta V > 0)$ then w < 0.

$$dw = -p_{ext}dV$$
 d means this is not an exact differential

Integral
$$W = -\int_{1}^{2} p_{ext} dV$$
 depends on the path!!!

• Path dependence of w

Example: assume a <u>reversible</u> process so that $p_{ext} = p$

Ar
$$(g, p_1, V_1)$$
 = Ar (g, p_2, V_2)
Compression $V_1 > V_2$ and $p_1 < p_2$





Two paths:

First $V_1 \rightarrow V_2$ at $p = p_1$ (2) First $p_1 \rightarrow p_2$ at $V = V_1$ then $p_1 \rightarrow p_2$ at $V = V_2$ then $V_1 \rightarrow V_2$ at $p = p_2$ (1)

 $Ar(g, p_1, V_1) = Ar(g, p_1, V_2) = Ar(g, p_2, V_2)$ $Ar(g, p_1, V_1) = Ar(g, p_2, V_1) = Ar(g, p_2, V_2)$





(Note w > 0, work done to compress it)

$$\boldsymbol{W}_{(1)} \neq \boldsymbol{W}_{(2)}$$
!!!

Note for the closed cycle [path (1)] - [path (2)], $\oint dw \neq 0$ — closed cycle <u>cannot</u> write w = f(p,V) wis not a state function

WORK

Work (w) is not a function of state. For a cyclic process, it is possible for $\oint dw \neq 0$



HEAT

That quantity flowing between the system and the surroundings that can be used to change the temperature of the system and/or the surroundings.

<u>Sign convention</u>: If heat enters the system, then it is <u>positive</u>.

Heat (q), like w, is a function of path. <u>Not</u> a state function

It is possible to have a change of state

 $(p_1, V_1, T_1) = (p_2, V_2, T_2)$

adiabatically (without heat transferred) or nonadiabatically.

Historically measured in calories [1 cal = heat needed to raise 1 g H₂O 1°C, from 14.5°C to 15.5°C]

The modern unit of heat (and work) is the Joule.

1 cal = 4.184 J





Joule showed that it's possible to raise the temperature of H_2O



Experimentally it was found that

$$\oint (\mathbf{d}\boldsymbol{w} + \mathbf{d}\boldsymbol{q}) = \mathbf{0}$$

 \Rightarrow The sum (*w* + *q*) is <u>independent of path</u>

⇒ This implies that there is a state function whose differential is dw + dq

We define it as U, the "internal energy" or just "energy"

 $\therefore \quad dU = dw + dq$

For a cyclic process $\oint dU = 0$

For a change from state 1 to state 2,

$$\Delta U = \int_{1}^{2} dU = U_{2} - U_{1} = q + w \quad \text{does not depend on path}$$

each depends on path individually, but not the sum

For fixed *n*, we just need to know 2 properties, e.g. (T, V), to fully describe the system.

So U = U(T, V)

U is an extensive function (scales with system size).

$$\overline{U} = \frac{U}{n}$$
 is molar energy (intensive function)



dU = dq + dwor Mathematical statement: $\Delta U = q + w$ or $-\oint dq = \oint dw$



$$\Delta U_{system} = q + w \qquad \Delta U_{surroundings} = -q - w$$
$$\Rightarrow \quad \Delta U_{universe} = \Delta U_{system} + \Delta U_{surroundings} = 0$$

<u>Clausius statement of 1st Law</u>:

The energy of the universe is conserved.